

```
>
> poly:=solve((a+b*z^2)^4=0,z);
```

$$poly := \frac{\sqrt{-b a}}{b}, -\frac{\sqrt{-b a}}{b}, \frac{\sqrt{-b a}}{b}, -\frac{\sqrt{-b a}}{b}, \frac{\sqrt{-b a}}{b}, -\frac{\sqrt{-b a}}{b}, \frac{\sqrt{-b a}}{b}, -\frac{\sqrt{-b a}}{b}$$

Resenim jsou dva ctyrnasobne koreny. Jelikož $a > 0$ a $b > 0$, tak se budu zajímat pouze o koren $\frac{\sqrt{-b a}}{b}$ (jeho imaginarní část je větší než nula). Podle pravidla na výpočet rezidua, spočtu reziduum v tomto ctyrnasobném polu.

```
> Pol:=sqrt(-b*a)/b;
> derivace:=diff(((z-Pol)^4*z^4)/((a+b*z^2)^4),z$3);
```

$$\begin{aligned} derivace := & \frac{24 \left(z - \frac{\sqrt{-b a}}{b} \right) z^4}{(a + b z^2)^4} + \frac{144 \left(z - \frac{\sqrt{-b a}}{b} \right)^2 z^3}{(a + b z^2)^4} - \frac{288 \left(z - \frac{\sqrt{-b a}}{b} \right)^2 z^5 b}{(a + b z^2)^5} \\ & + \frac{144 \left(z - \frac{\sqrt{-b a}}{b} \right)^3 z^2}{(a + b z^2)^4} - \frac{864 \left(z - \frac{\sqrt{-b a}}{b} \right)^3 z^4 b}{(a + b z^2)^5} + \frac{960 \left(z - \frac{\sqrt{-b a}}{b} \right)^3 z^6 b^2}{(a + b z^2)^6} \\ & + \frac{24 \left(z - \frac{\sqrt{-b a}}{b} \right)^4 z}{(a + b z^2)^4} - \frac{384 \left(z - \frac{\sqrt{-b a}}{b} \right)^4 z^3 b}{(a + b z^2)^5} + \frac{1200 \left(z - \frac{\sqrt{-b a}}{b} \right)^4 z^5 b^2}{(a + b z^2)^6} \\ & - \frac{960 \left(z - \frac{\sqrt{-b a}}{b} \right)^4 z^7 b^3}{(a + b z^2)^7} \end{aligned}$$

```
> derivace:=simplify(%);
```

$$\begin{aligned} derivace := & -24(-b z + \sqrt{-b a}) z (-34 b a^3 \sqrt{-b a} z^2 + 90 b^2 a^2 \sqrt{-b a} z^4 + z^8 b^4 \sqrt{-b a} \\ & + 9 z^7 b^4 a - 34 b^3 a \sqrt{-b a} z^6 + a^4 \sqrt{-b a} - 9 b z a^4 + 71 z^3 b^2 a^3 - 71 z^5 b^3 a^2) / (b^3 \\ & (a + b z^2)^7) \end{aligned}$$

```
> Reziduum:=(1/6)*limit(derivace,z=Pol);
```

$$Reziduum := -\frac{\sqrt{-b a}}{32 a^2 b^3}$$

```
>
> Integral:=(1/2)*(2*Pi*I*Reziduum);
```

$$Integral := \frac{\frac{-1}{32} I \pi \sqrt{-b a}}{a^2 b^3}$$

Protože $a > 0$ a $b > 0$, je možno psát $Integral = \frac{1 \pi}{32 b^2 a \sqrt{ab}}$

```
> simplify(1/32*Pi/(b^2*a*sqrt(ab)));
```

$$\frac{\pi}{32 b^2 a \sqrt{ab}}$$

```
>
```

```
>
```