

FOURIEROVY ŘADY

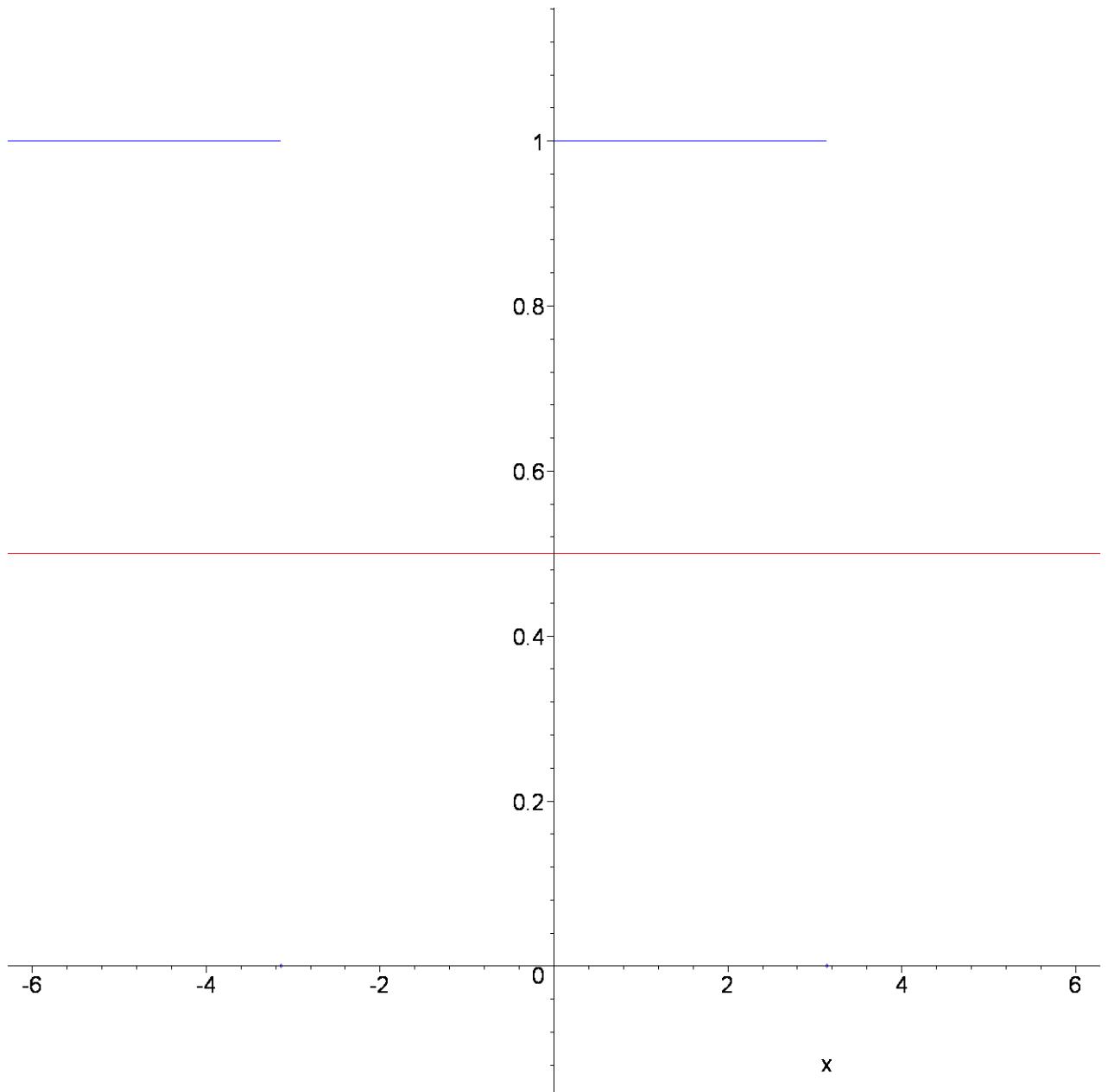
Zde je možné si prohlédnout ...

Použití : vybrat myší EDIT (nahoře na liště)

vybrat myší EXECUTE (v rozvinuté nabídce)

vybrat myší WORKSHEET (v rozvinuté nabídce)

... to spustí výpočet a zobrazí postupně všechny grafy.



```
>
> funkce (x) = a(0)/2 + Sum((aaa(n)*cos(n*x) +
   bbb(n)*sin(n*x)),n=1..m) ;
```

$$\begin{aligned} & \left\{ \begin{array}{ll} 1 & x < \pi \\ 0 & \pi < x \end{array} \right. = \frac{1}{2} + \left(\sum_{n=1}^{30} \left(\begin{aligned} & (0, 0) \\ & \left. \cos(n x) + \left(\begin{aligned} & \frac{2}{3\pi}, 0, \frac{2}{5\pi}, 0, \frac{2}{7\pi}, 0, \frac{2}{9\pi}, 0, \frac{2}{11\pi}, 0, \frac{2}{13\pi}, 0, \frac{2}{15\pi}, 0, \frac{2}{17\pi}, 0, \frac{2}{19\pi}, 0, \frac{2}{21\pi}, 0, \frac{2}{23\pi}, 0, \\ & \frac{2}{25\pi}, 0, \frac{2}{27\pi}, 0, \frac{2}{29\pi}, 0 \end{aligned} \right) \right. \\ & \left. \sin(n x) \right) \right) \end{aligned} \right. \end{aligned}$$

PARSEVAL :

```
> Int((Funkce(x))^2,x=0..2*Pi)/Pi = A(0)^2/2 + Sum(A(n)^2
+ B(n)^2,n=1..m);
```

$$\frac{1}{\pi} \int_0^{2\pi} \text{Funkce}(x)^2 dx = \frac{1}{2} A(0)^2 + \left(\sum_{n=1}^{30} (A(n)^2 + B(n)^2) \right)$$

```
> int((funkce(x))^2,x=0..2*Pi)/Pi = a(0)^2/2 + Sum((aaa(n))^2
+ (bbb(n))^2,n=1..m);
```

>

>

Funkce x na intervalu $(-\pi, \pi)$:

```
> funkce:=x -> piecewise(x<Pi,x/2,x>Pi,x/2 - Pi);
```

$$funkce := x \rightarrow \text{piecewise}\left(x < \pi, \frac{1}{2}x, \pi < x, \frac{1}{2}x - \pi\right)$$

```
> funkce (x) = a(0)/2 + sum(a(n)*cos(n*x)) +  
b(n)*sin(n*x),n=1..m) ;
```

$$\begin{cases} \frac{x}{2} & x < \pi \\ \frac{x}{2} - \pi & \pi < x \end{cases} = -\frac{1}{16} \sin(16x) + \frac{1}{5} \sin(5x) + \frac{1}{9} \sin(9x) - \frac{1}{12} \sin(12x) - \frac{1}{6} \sin(6x) + \frac{1}{29} \sin(29x) + \frac{1}{27} \sin(27x) - \frac{1}{24} \sin(24x) - \frac{1}{30} \sin(30x) - \frac{1}{28} \sin(28x) - \frac{1}{26} \sin(26x) + \frac{1}{23} \sin(23x) + \frac{1}{13} \sin(13x) - \frac{1}{22} \sin(22x) + \frac{1}{21} \sin(21x) + \frac{1}{17} \sin(17x) - \frac{1}{18} \sin(18x) + \frac{1}{11} \sin(11x) + \frac{1}{15} \sin(15x) + \frac{1}{19} \sin(19x) - \frac{1}{8} \sin(8x) - \frac{1}{20} \sin(20x) + \frac{1}{25} \sin(25x) + \frac{1}{7} \sin(7x) + \sin(x) - \frac{1}{2} \sin(2x) + \frac{1}{3} \sin(3x) - \frac{1}{4} \sin(4x) - \frac{1}{10} \sin(10x) - \frac{1}{14} \sin(14x)$$

```
[> x = Sum ((-1)^(n+1)*sin(n*x)/n,n=1..infinity);
```

$$x = \sum_{n=1}^{\infty} \frac{(-1)^{(n+1)} \sin(n x)}{n}$$

[to byl rozvoj a toto je Parseval :

```
[> Pi^2/6 = Sum (1/n^2,n=1..infinity);
```

$$\frac{\pi^2}{6} = \sum_{n=1}^{\infty} \frac{1}{n^2}$$

[>

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